Experimental approach for evaluating uncertainties associated to stationary vehicle noise according to ISO 5725

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Introduction

Determination of uncertainties related to the standard ISO 5130 (Measurements of sound pressure level emitted by stationary road vehicles near the exhaust systems)

Analysis based on the use of the ISO 5725 approach

Uncertainties estimated on different conditions:

- run-to-run (with several operators)
- day-to-day (Atmospheric condition)
- site-to-site (surface condition)
- vehicle to vehicle



Context

European regulation (directive 1999/101/CE and the regulation 51 rev02) presents two acoustical tests:

- A dynamic test which is subject to limit
- A stationary test

The stationary test is also used by national authorities to control vehicle in use:

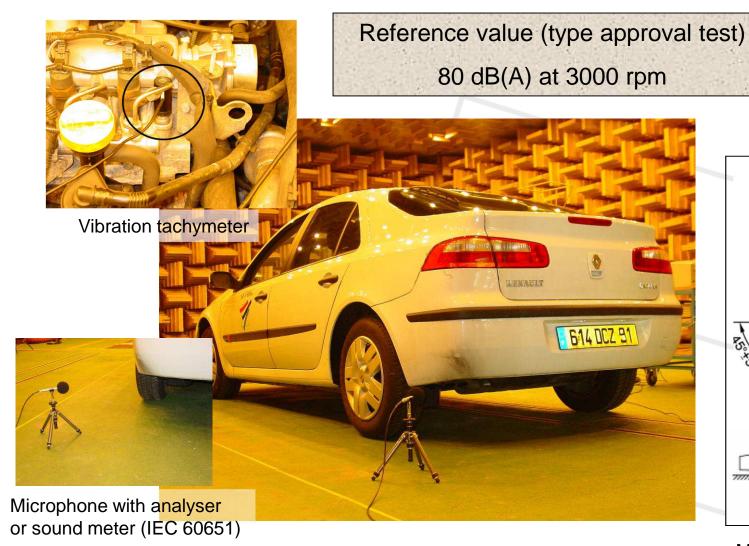
- Spot test by police
- Periodical test by technical inspection facilities

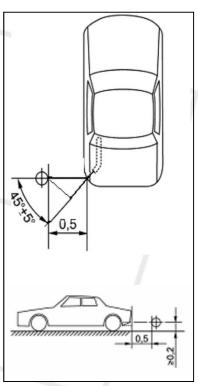
The stationary test is based on the international standard ISO 5130

French regulation allows a 5 dB divergence between type approval and in use test values



Measuring procedure

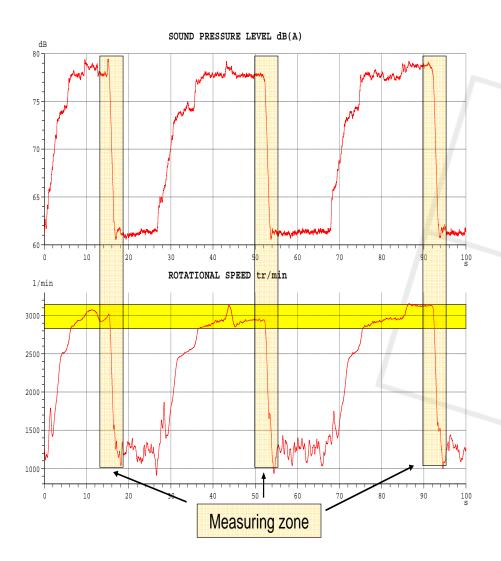




Microphone position



Measuring procedure



Conditions of engine operation:

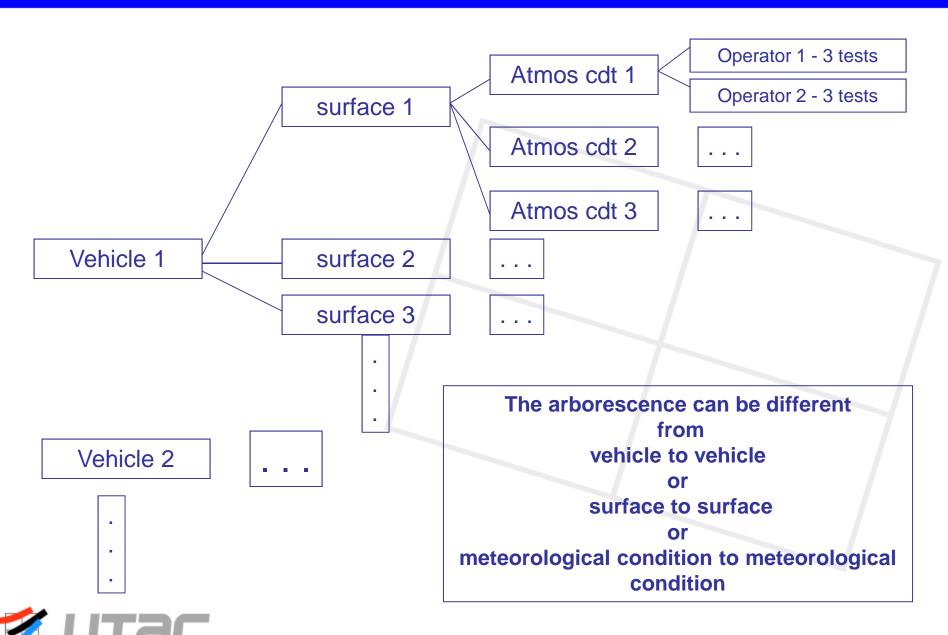
- Engine speed stabilized at a reference value
- Throttle rapidly returned to the idling position.

Conditions of acoustical measurement:

- Sound level measured over this operating period
- Maximum sound-level meter reacting being taken as the test result (dB(A) – FAST)
- Three measurements
- Final result is the mean these 3 values



Structure of the study



Estimation of the uncertainty of measurement

- Definition
- GUM approach
- •ISO 5725 approach



Definition (1)

• Estimation of the range which contains the **true value** (VIM 1984)

 Parameter, associated with the result of a measurement that characterizes the <u>dispersion</u> of the value that could reasonably be attributed to the measurement (VIM 3.9 1993)



Definition (3)

 Coverage interval: GUM 2.3.5 "interval that may be expected to encompass a large fraction of the distribution of values that could reasonably be attributed to the measurand.

$$[y-ku_c(y), y+ku_c(y)]$$



Two approaches

- "GUM approach"
- "ISO 5725 approach"

These two approaches are complementary and are not exclusive. In both cases variances estimates are calculated. Furthermore it's possible to use the two approaches together.



GUM approach (1)

$$Y = f(X_1, X_2, ..., X_n)$$

- Y is determined from n other quantities
- Representation of a process of measurement
- First-order Taylor series approximation

$$\sigma_{\mathbf{Y}}^{2} = \sum_{i=1}^{n} \left(\frac{\partial \mathbf{f}}{\partial \mathbf{X}_{i}} \right)^{2} \sigma_{\mathbf{X}_{i}}^{2} + 2 \sum_{i=1}^{n-1} \sum_{j=i+1}^{n} \frac{\partial \mathbf{f}}{\partial \mathbf{X}_{i}} \frac{\partial \mathbf{f}}{\partial \mathbf{X}_{j}} \sigma_{\mathbf{x}_{i}} \sigma_{\mathbf{x}_{j}} \rho_{ij}$$



GUM approach (2)

- It is necessary to find the functional relationship f
- Not exhaustive
- suited for metrology/calibration rather than tests laboratories
- Ascending approach



ISO 5725 approach (1)

Accuracy of measurement method.

- Precision

- Trueness



ISO 5725 approach (2)

- Precision: the closeness of agreement between independent test results obtained under stipulated conditions.
 - Repeatability: precision under repeatability conditions, expressed by a standard deviation.
 - Reproducibility: precision under reproducibility conditions expressed by a standard deviation.
- Trueness: the closeness of agreement between the average value from a large series of test results and an accepted reference value.
 - The measure of trueness is expressed in terms of bias



ISO 5725 approach (4)

Model of analysis of variance:

$$Y_{ij} = m + L_{i} + \epsilon_{ij} \label{eq:Yij}$$
 where

 Y_{ij} jth test result from laboratory i,

m general mean,

 L_{i} laboratory effect i, i=1 to p, with variance σ_{I}^{2}

 \mathcal{E}_{ij} residue on the jth result from laboratory i, j = 1 to n, σ_{ϵ}^2



ISO 5725 approach (5)

| Effects | Sum of square | Degree of freedom | Mean square | Expected |
|------------|---|-------------------------|---|--|
| Laboratory | $\sum_{i=1}^{i=p} \sum_{j=1}^{j=n} (\overline{y}_i - \overline{y})^2 = B$ | p-1 | $\sum_{i=1}^{i=p} \sum_{j=1}^{j=n} (\overline{y}_i - \overline{y})^2 / p - 1$ | $n\sigma_L^2 + \sigma_{\varepsilon}^2$ |
| Residual | $\sum_{i=1}^{i=p} \sum_{j=1}^{j=n} (y_{i,j} - \overline{y}_i)^2 = W$ | np – p | $\sum_{i=1}^{i=p} \sum_{j=1}^{j=n} (y_{i,j} - \overline{y}_i)^2 / np - p$ | σ_{ϵ}^2 |
| Total | $\sum_{i=1}^{i=p} \sum_{j=1}^{j=n} (y_{i,j} - \overline{y})^2 = T$ | np-1 | | |





ISO 5725 approach (6)

Precision evaluation :

- ⇒ Variance components estimation

$$S_r = S_{\varepsilon}$$
 $S_R = \sqrt{S_{\varepsilon}^2 + S_L^2}$

Trueness evaluation :

- $-\delta = m \mu$ where μ is the reference value when it exists.
- Estimated by : $\hat{\mathcal{S}} = \hat{\mathbf{m}} \mu$



ISO 5725 approach (7)

Our model is more complicated

$$\boldsymbol{y}_{ijklm} = \boldsymbol{\mu} + \boldsymbol{V}_i + \boldsymbol{A}\boldsymbol{C}_j(\boldsymbol{V}_i) + \boldsymbol{T}\boldsymbol{S}_k(\boldsymbol{A}\boldsymbol{C}_j(\boldsymbol{V}_i)) + \boldsymbol{O}_l(\boldsymbol{T}\boldsymbol{S}_k(\boldsymbol{A}\boldsymbol{C}_j(\boldsymbol{V}_i))) + \boldsymbol{\epsilon}_{ijklm}$$

represents the value of the studied characteristic of the mth repetition for the \mathbf{y}_{ijklm} Ith operator of kth test surface of jth atmospheric condition of ith vehicle,

μ

the effect due to ith vehicle, presumed distributed according to a Laplace-Gauss distribution with mean 0 and variance σ_v^2

 $AC_i(V_i)$ effect due to the j^{th} atmospheric condition of i^{th} vehicle, presumed distributed according to a Laplace-Gauss distribution with mean 0 and variance σ_{AC}^2

$$TS_k(AC_j(V_i))$$
 σ_{TS}^2

$$O_l(TS_k(AC_j(V_i))) \ \sigma_o^2$$



residue of the surface jth atm and variance residue of the mth repetition for the lth operator of kth test surface jth atmospheric condition of ith vehicle, with mean 0 Copyright UTAC

ISO 5725 approach (8)

Estimation of the variance components

$$s_r = s_{\varepsilon}$$

$$s_{fi(1)} = \sqrt{s_r^2 + s_o^2}$$

$$s_{fi(2)} = \sqrt{s_r^2 + s_O^2 + s_{TS}^2}$$

$$s_{fi(3)} = \sqrt{s_r^2 + s_O^2 + s_{TS}^2 + s_{AC}^2}$$

$$s_R = \sqrt{s_r^2 + s_O^2 + s_{TS}^2 + s_{AC}^2 + s_V^2}$$



ISO 5725 approach (9)

- the combined standard uncertainty u_c(y) comes from the values of precision:
- in conditions of repeatability, $u_c(y) = s_r$
- in conditions of intermediate precision, $u_c(y) = s_{fi}$
- in conditions of reproducibility $u_c(y) = s_R$
- the expanded uncertainty. $U = k \times u_c(y)$



ISO 5725 approach (10)

| | Stationary Noise | | | |
|--|---------------------|--|--|--|
| studied characteristic | | | | |
| Ctan danid daniation of manageralities with apprehent with a | $(in \ dB(A))$ | | | |
| Standard deviation of repeatability, with constant vehicle, | 0.3 | | | |
| atmospheric condition, test surface and operator Limit of repeatability, with constant vehicle, atmospheric | | | | |
| condition, test surface and operator | 0.8 | | | |
| Expanded uncertainty in conditions of repeatability, with | | | | |
| constant vehicle, atmospheric condition, test surface and | 0.6 | | | |
| operator | 0.0 | | | |
| Intermediate standard deviation of precision, with constant | | | | |
| vehicle, atmospheric condition and test surface, whatever the | 0.4 | | | |
| operator | 0.4 | | | |
| Intermediate limit of precision, with constant vehicle, | 1.1 | | | |
| atmospheric condition and test surface, whatever the operator | | | | |
| Expanded uncertainty in conditions of intermediate | | | | |
| precision, with constant vehicle, atmospheric condition and | 0.8 | | | |
| test surfaces, whatever the operator | 0.0 | | | |
| Intermediate standard deviation of precision, with constant | 0.5 | | | |
| vehicle and atmospheric condition, whatever the test surface and | | | | |
| the operator | | | | |
| Intermediate limit of precision, with constant vehicle and | 1.5 | | | |
| atmospheric condition, whatever the test surface and the operator | | | | |
| Expanded uncertainty in conditions of intermediate | | | | |
| precision, with constant vehicle and condition atmospheric, | 1.1 | | | |
| whatever the test surface and the operator | | | | |
| Intermediate standard deviation of precision, with constant | | | | |
| vehicle, whatever the atmospheric condition, the test surface and | 0.5 | | | |
| the operator | | | | |
| Intermediate limit of precision, with constant vehicle, whatever | 1.5 | | | |
| the atmospheric condition, the test surface and the operator | | | | |
| Expanded uncertainty in conditions of intermediate | // | | | |
| precision, with constant vehicle, whatever the atmospheric | 1.1 | | | |
| condition, the test surface and the operator | | | | |
| Standard deviation of reproducibility, whatever the vehicle, the | 1.0 | | | |
| atmospheric condition, the test surface and the operator | | | | |
| Limit of reproducibility, whatever the vehicle, the atmospheric | 2.8 | | | |
| condition, the test surface and the operator | | | | |
| Expanded uncertainty in conditions of reproducibility, | | | | |
| whatever the vehicle, atmospheric condition, the test surface | 2.0 | | | |
| and the operator | | | | |



ISO 5725 approach (11)

Better suited for test laboratories

- -use of the data which are available
- use of the precision value issued from interlaboratories test

Descending approach



Thank you for attention



Standardization works

- ISO/TC 69/SC 6
 - WG 1 Accuracy of measurement methods and results
 - WG 5 Limits of determination
 - WG 7 Statistical methods to support measurement uncertainty evaluation.
- JCGM/WG1
 - WG1 Measurement uncertainty (VIM GUM)

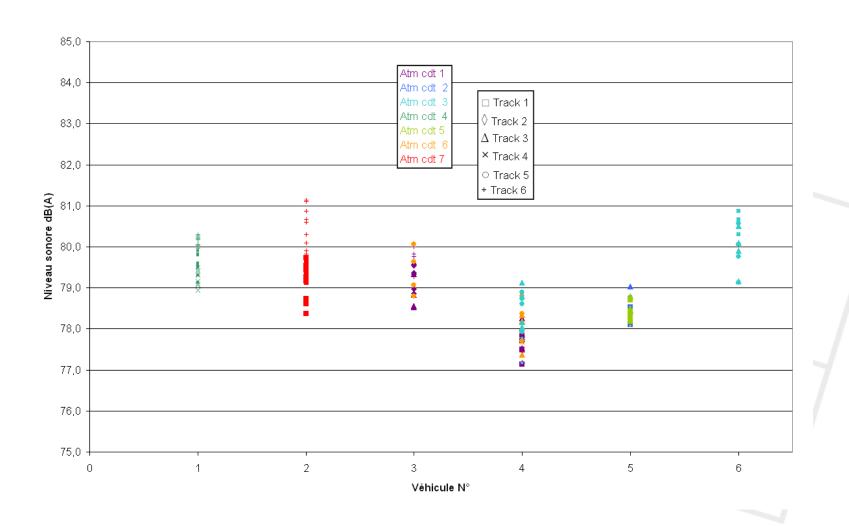


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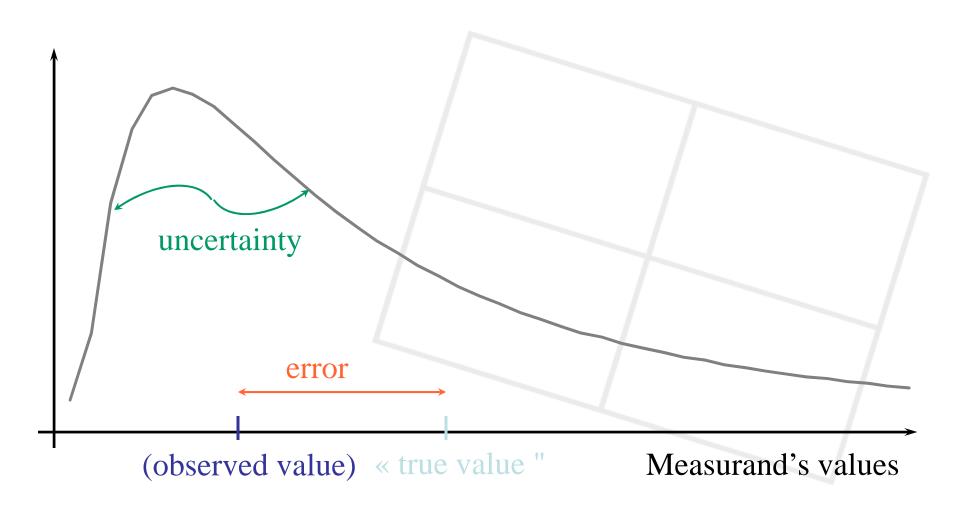


Experimental results





Measurand, Error, Uncertainty





ISO 5725 approach (3)

